

# Fair Background Data Transfers of Minimal Delay Impact

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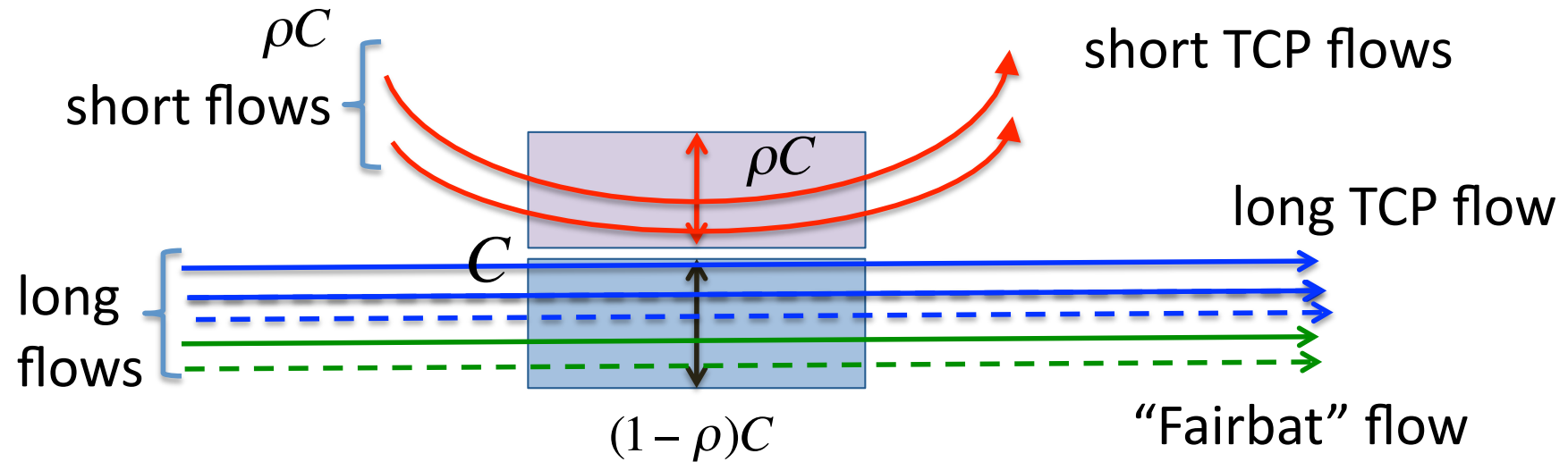
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- Propose a framework for the design of protocols for background transfers
- File sizes differ by  $>10$  orders of magnitude, connection rates by few orders of magnitude
- Main concern: how to obtain reasonable throughput with minimal delays on short flows
- Current approaches: TCP-nice, LEDBAT,...
  - behave as second priority traffic (low impact on short flows)
  - no consideration of fairness relative to other long flows
  - no adoption incentives
- Related work: Key, Massoulié, etc.
  - substitution of **all** long TCPs by on-off senders based on **threshold price**
  - prove that there is *some* delay improvement
  - mostly a different traffic model, assumes all flows to convert to new protocol

# The competition environment



- No competing long TCP: easy case!! FB: 2<sup>nd</sup> priority
- 1 long TCP: FB 2<sup>nd</sup> priority => zero throughput
- existing solutions: > 2<sup>nd</sup> priority, unspecified throughput

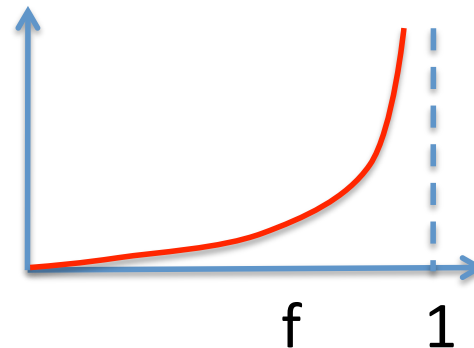
# Adoption incentives vs “niceness”

- Why “long TCP” users adopt FB instead of TCP?
- Which are sensible properties of FBs?
  - When competing with long TCPs for  $C(1 - \rho)$ :
    - obtain a **given** fraction  $f$  of  $C(1 - \rho)$ ,
    - cause **minimum extra delays** on short flows
  - Example: obtain same average throughput as TCP  $f = \frac{l}{k+l}$
- Achieve all that with reasonable context information
  - public Internet context, competition with non-local flows

# Our results

- Obtain optimal BW sharing policy under **complete information**
  - minimize delays on short flows while competing with  $k$  long TCPs and obtaining a share  $f$  of the leftover capacity
- Implementable approximation: weighted TCP
  - short time scales: use  $w$ -TCP  $f = \frac{w}{k+w}$
  - delay deterioration  $\leq 17.2\%$  for  $k = 1$ ,  
 $\downarrow 0$  as  $k \rightarrow \infty$

- Delay impact  $\delta(f)$



# Our results (cont.)

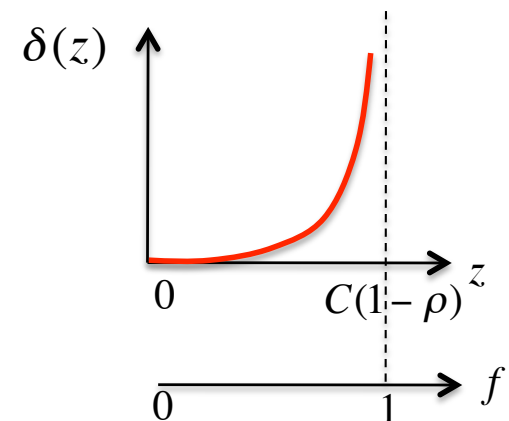
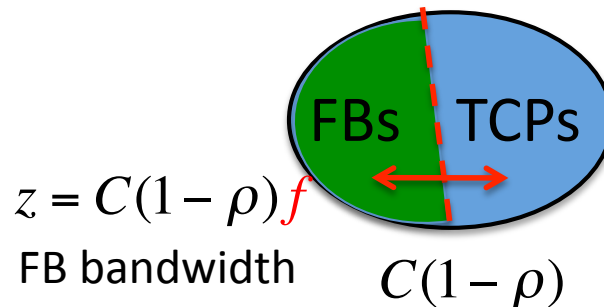
- Adopt Kelly's approach for fairness, but for long-term
  - FBs **don't get a fixed fraction  $f$**  of leftover capacity
  - max some social welfare function
    - sum of utilities for average throughput of long flows TCPs, FBs
    - add a negative externality term (extra delay to short flows)
  - **implementation**: using w-TCPs
    - don't need to know  $k, C, \rho, \dots$
- Use this framework to design new protocols
  - examples:  $y_0 / y_i = 1 + \gamma y_0^{-1}$   
 $y_0 / y_i = 1 + \gamma y_0$

# A corollary

- If we substitute any subset of long TCP flows by “equivalent” optimal FBs, the max improvement of the delay of short flows is less than 17.2%
- The best improvement is achieved when there is competition of 1FB and 1 long TCP flow
- A negative result?
- The incentive compatibility constraint (obtain same average throughput as TCP) in larger systems implies small optimal delay improvements
- To get significant delay improvement we need to relax the IC condition (how?)

# The general fairness framework

- Problem: “fair” share of excess capacity
- Express fairness on long-term rates “à la Kelly”
- Take into account delay spillovers to short flows
  - remember the tradeoff  $f \leftrightarrow$  delay
- Engineering: translate into flow control algorithms
  - decompose controls for short and long timescales
  - make reasonable assumptions on what is known locally
- Reverse engineering: translate existing algorithms into this model





# The optimization problem

$$\max \quad ku_0(y_0) + \sum_{i=1}^l u_i(y_i) - \int_0^{\sum_{i=1}^l y_i} \delta \left( \sum_{i=1}^n x_i \right) F(\delta(z)) dz$$

$$\text{such that } ky_0 + \sum_{i=1}^l y_i = C(1 - \rho),$$

$$\text{over } y_0, \dots, y_l \geq 0$$

Assume that w-TCP is used  
in the short t.s. Then magic!!!

$$\delta_w \left( \sum_{i=1}^l y_i \right) = \frac{1}{y_0}$$

$$\text{Optimality condition for long ts: } -u'_0(y_0) + u'_i(y_i) - \frac{1}{y_0^2} F \left( \frac{1}{y_0} \right) = 0, i = 1, \dots, l$$

Short ts: use w-TCP	Long ts: adapt the weights	$\dot{w}_i = -u'_0 \left( \frac{y_i}{w_i} \right) + u'_i(y_i) - \left( \frac{w_i}{y_i} \right)^2 F \left( \frac{w_i}{y_i} \right), i = 1, \dots, l$
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# Engineering new protocols

$$\begin{aligned} \max \quad & ku_0(y_0) + \sum_{i=1}^l u_i(y_i) - \int_0^{\sum_{i=1}^l y_i} \delta_w(z)^2 F(\delta(z)) dz & -u'_0(y_0) + u'_i(y_i) - \frac{1}{y_0^2} F\left(\frac{1}{y_0}\right) = 0, i = 1, \dots, l \\ \text{such that} \quad & ky_0 + \sum_{i=1}^l y_i = C(1 - \rho), & \Leftrightarrow \dot{w}_i = -u'_0\left(\frac{y_i}{w_i}\right) + u'_i(y_i) - \left(\frac{w_i}{y_i}\right)^2 F\left(\frac{w_i}{y_i}\right), i = 1, \dots, l \\ \text{over } & y_0, \dots, y_l \geq 0, \text{ w-TCP short ts controls} \end{aligned}$$


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Case A:

$$u_i(y) = \log y, i = 0, \dots, l, F(\delta) = \gamma$$

$$\frac{y_0}{y_i} = 1 + \gamma y_0^{-1}, i = 1, \dots, l$$

Case B:

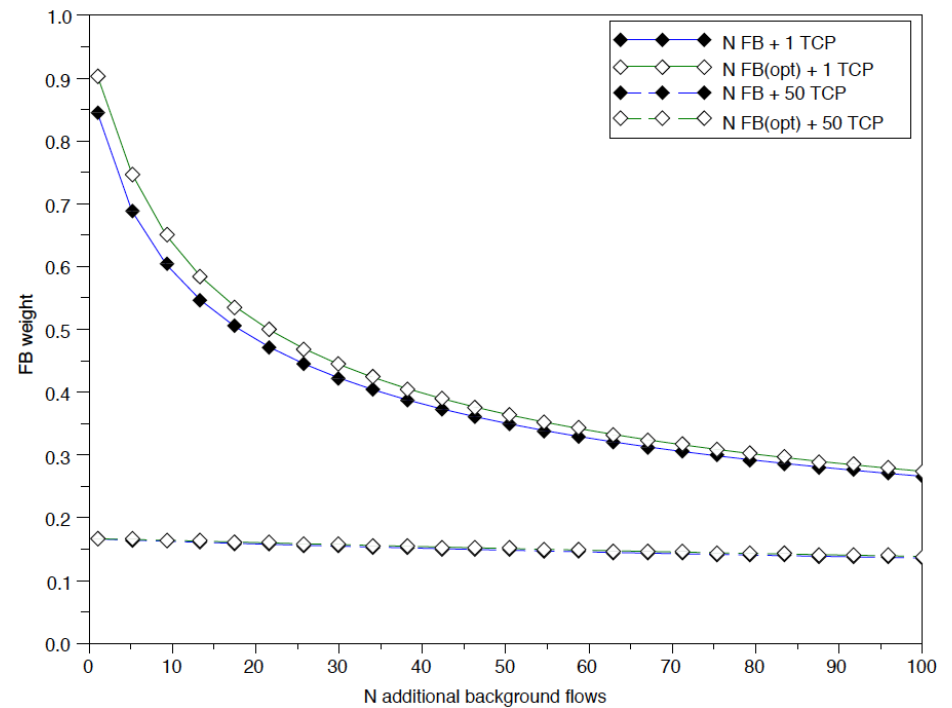
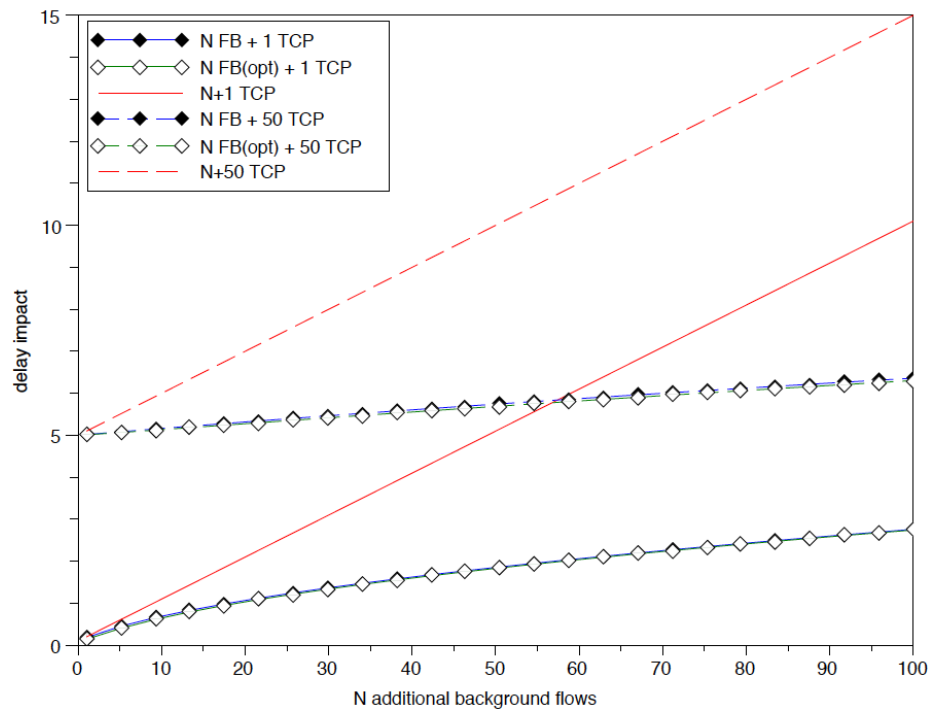
$$u_i(y) = \log y, i = 0, \dots, l, F(\delta) = \gamma \delta^{-2}$$

$$\frac{y_0}{y_i} = 1 + \gamma y_0, i = 1, \dots, l$$

# Algorithm A

$$\frac{y_0}{y_i} = 1 + \gamma y_0^{-1}, i = 1, \dots, l$$

- FBs get similar throughput as TCP when there is enough excess bandwidth, give away when it becomes scarce
- IC condition relaxed when resources are scarce (second priority when sensible)



# Conclusions

- Protocols for background transfers operate in the context of other long and short TCP flows
- TCP is the incumbent protocol, new protocols should compare to TCP
- We derived the optimal short time scale policy for achieving a given share of long term throughput, but has practical implementation issues
- w-TCP seems a reasonable practical alternative, provably small efficiency loss
- We provided a utility-based definition for fair sharing including a negative externality term for delay caused to short flows
- We derived two new interesting protocols for background transfers by relaxing the IC condition for adoption relative to TCP